

## Trigonometry

1. a)  $\pi/2$  e)  $180^\circ$   
 b)  $\pi/3$  f)  $45^\circ$   
 c)  $\pi/180$  g)  $120^\circ$   
 d)  $2\pi/3$  h)  $180^\circ$

2. a)

$a$	$b$	$c$	$\alpha$	$\beta$	$\gamma$
3cm	5,2cm	6cm	$30^\circ$	$60^\circ$	$90^\circ$
1,9cm	18,1cm	18cm	$6^\circ$	$90^\circ$	$84^\circ$
16.6cm	13.1cm	10,2cm	$90^\circ$	$52^\circ$	$38^\circ$
12,3cm	27.1cm	24.1cm	$27^\circ$	$90^\circ$	$63^\circ$

- b) i.  $a = 8mm$  (gegeben),  $b = 8,4mm$  (gegeben),  $c = 2,56122mm$   
 ii.  $a = 5,77169m$ ,  $b = 3,5m$  (gegeben),  $c = 6,75m$  (gegeben)  
 iii.  $a = 3,4m$  (gegeben),  $b = 1,82182m$ ,  $c = 2,8707m$   
 iv.  $a = 3,98785cm$ ,  $b = 6,22293cm$ ,  $c = 8,3cm$  (gegeben)  
 v.  $a = 6,7mm$  (gegeben),  $b = 12,0423mm$ ,  $c = 15,4848mm$   
 vi.  $a = 7,2cm$  (gegeben),  $b = 5,1cm$  (gegeben),  $c = 4,33cm$

$$3. \quad a) \quad \frac{\sin(2\alpha)}{1 + \cos(2\alpha)} = \frac{2 \sin(\alpha) \cos(\alpha)}{1 + \cos^2(\alpha) - \sin^2(\alpha)} = \frac{2 \sin(\alpha) \cos(\alpha)}{1 + 2 \cos^2(\alpha) - 1} = \frac{2 \sin(\alpha) \cos(\alpha)}{2 \cos^2(\alpha)} = \frac{\sin(\alpha)}{\cos(\alpha)} = \tan(\alpha)$$

For the denominator we use:  $\cos(2\alpha) = \cos^2(\alpha) - \sin^2(\alpha) = 2 \cos^2(\alpha) - 1 = 1 - 2 \sin^2(\alpha)$

$$b) \quad (1 + \cos(2\alpha))(1 - \sqrt{1 - \sin^2(2\alpha)}) = (1 + \cos(2\alpha))(1 - \cos(2\alpha)) = 1 - \cos^2(2\alpha) = \sin^2(2\alpha)$$

**OR:**

$$(1 + \cos(2\alpha))(1 - \sqrt{1 - \sin^2(2\alpha)}) = (1 + \cos(2\alpha))(1 - \cos(2\alpha)) = 2 \cos^2(\alpha) 2 \sin^2(\alpha) = 4 \cos^2(\alpha) \sin^2(\alpha) = \sin^2(2\alpha)$$

4. Applying the addition theorems for sine and cosine results in

$$\begin{aligned}\sin((x + y) + z) &= \sin(x + y) \cos(z) + \cos(x + y) \sin(z) \\ &= (\sin(x) \cos(y) + \cos(x) \sin(y)) \cos(z) + \\ &\quad (\cos(x) \cos(y) - \sin(x) \sin(y)) \sin(z) \\ &= \sin(x) \cos(y) \cos(z) + \cos(x) \sin(y) \cos(z) + \\ &\quad \cos(x) \cos(y) \sin(z) - \sin(x) \sin(y) \sin(z).\end{aligned}$$